

COMMENTS AND CRITICISM

STOPPING TO REFLECT*

Our note is prompted by a recent article by Frank Arntzenius, "Some Problems for Conditionalization and Reflection."¹ Through a sequence of examples, that article purports to show limitations for a combination of two inductive principles that relate current and future rational degrees of belief: *Temporal Conditionalization* and *Reflection*:

agent's corpus of knowledge changes between *now* and *later* solely by

restrictions or limitations beyond what is already assumed as familiar in problems of stochastic prediction.

To the extent that a rational person does not know *now* exactly what she or he will know in the future, anticipating one's future

to form a filtration, not as his Terms and Conditions. It is

satisfied (as its antecedent fails), but then Reflection fails unless what
is forgotten in the failure of filtration becomes practically certain. It

Time is indexed for the agent by 1 1 0 1

value of $P_{later}(A)$ and knowing it is this quantity, one may calculate T exactly and thus know the outcome of the $n+1^{st}$ toss which is heads

then know that *later* has arrived. Thus, *later*, he is not in a position to use the extra information that he would get from knowing when T

or if $A = H_i$ then $y_t(A) = \frac{P_{now}(H_t | P_{later}(A) = r)}{P_{now}(H_t | P_t(A) = r)} = 1$. Thus, $P_{now}(A | P_{later}(A) = r) = r$. That is, even though *later* is not a stopping time, Reflection holds in this case since, given that $P_{later}(A) = r$, no new (relevant) evidence about A is conveyed through knowing that *later*

value $E_p(X|C)$ exist with respect to the probability P . Let A be an event and let $X = P(A|Y)$ be a random variable, a function of the random variable Y . Then, as a consequence of the law of total probability, with C also a function of Y ,

$$(1.1) \quad P(A|C) = E_p [X|C].$$

Assume that the agent's degrees of belief *now* include his *later* degrees of belief as objects of uncertainty. That is, future events such

as " $P(A) = r$ " and " $P(A|C) = d$ " are proper subjects *now* of the

agent's current degrees of belief. Suppose that, *now*, the agent anticipates using (i) Temporal Conditionalization in responding to the new evidence $Y = v$ that he knows he will learn at the stopping time. Let E

this is known to happen at t . Since $P_t(E) \in (0,1)$...

not change this value, that is,

$$(2.1) \quad P_{t_1}(E) = P_{t_1}(E | P_{t_2}(E) = r)$$

for a set of r -values of probability 1 under P_{t_1} . But, since it is known at t_1 that E will be forgotten at t_2 , $P_{t_1}(0 < P_{t_2}(E) < 1) = 1$. Hence Reflection fails as $0 < r < 1$ in (2.1).

Proof of Result 3. Assume that the agent's information sets form a filtration over time and that Temporal Conditionalization holds between *now* and *later* but that *later* is not a stopping time for the